

### Amendments To The Claims.

1. (Currently Amended) Gradient tensor induction magnetic field measuring apparatus for measuring ~~the~~ a gradient tensor induction magnetic signal of ~~the~~ a transient magnetic field in a ~~borehole~~ wellbore to be used to determine ~~the~~ a conductivity gradient of ~~the~~ an anisotropic earth formations penetrated by a the wellbore, the apparatus comprising e, f and any or any combination of a)-d), wherein:
  - a) at least one transmitter coil and a pair of closely located parallel tri-axial EM induction receivers, each formed by three mutually orthogonal receiver coils, separated by a small vector,  $\Delta r$ , wherein ~~the~~ a distance between the two parallel tri-axial EM induction receivers is much smaller than ~~the~~ a distance  $L$  between the transmitter and ~~the~~ a center of the vector  $\Delta r$ , connecting the two ~~receivers~~:  ~~$\Delta r \ll L$~~ , ~~in order that the~~ receivers, wherein conditions are fulfilled that the gradients are measured of ~~the~~ different components of the magnetic field induced in the earth formation;
  - b) at least one receiver coil and a pair of closely located parallel tri-axial EM induction transmitter coils, separated by a small vector,  $\Delta r$ , wherein ~~the~~ a distance between the two parallel tri-axial EM induction transmitters is much smaller than ~~the~~ a distance  $L$  between the receiver and ~~the~~ a center of the vector  $\Delta r$ , connecting the two ~~transmitters~~:  ~~$\Delta r \ll L$~~ , ~~in order that the~~ transmitters, wherein conditions are fulfilled, based on ~~the~~ a reciprocity principal, that ~~the~~ gradients are measured of ~~the~~ different components of the magnetic field induced in the earth formation;
  - c) a tri-axial EM induction transmitter formed by three mutually orthogonal transmitter coils, and a pair of closely located tri-axial EM induction receivers, each formed by

three mutually orthogonal receiver coils, separated by a small vector,  $\Delta \mathbf{r}$ , wherein ~~the~~ a distance between the two tri-axial EM induction receivers is much smaller than the ~~a distance  $L$  between the tri-axial transmitter and the a center of the  $\Delta \mathbf{r}$ ,  $\Delta \mathbf{r} \ll L$ , in~~ order that the wherein conditions are fulfilled that ~~the~~ the gradients are measured of ~~the~~ different components of the induction tensor formed by the magnetic fields induced in the earth formation;

- d) a pair of closely located tri-axial EM induction transmitters, separated by a small vector,  $\Delta \mathbf{r}$ , and a tri-axial EM induction receiver, wherein ~~the~~ a distance between two tri-axial EM induction transmitters is much smaller than the distance  $L$  between the tri-axial receiver and the center of the vector  $\Delta \mathbf{r}$ ,  ~~$\Delta \mathbf{r} \ll L$ , in order that the~~ wherein conditions are fulfilled, based on ~~the~~ a reciprocity principal, ~~that the~~ gradients are measured of ~~the~~ different components of the induction tensor formed by the magnetic fields induced in the earth formation; and
- e) means for receiving voltages induced in said receiver coils;
- f) means for measuring a difference between the said voltages in the different pairs of the receivers, or due to the different pairs of the transmitters.

2. (Currently Amended) The apparatus as defined in claim 1 further comprising:

- a) a tri-axial transmitter array and three pairs of receiver coils, measuring ~~the~~  $\partial H_z^\beta / \partial x$ ,  $\partial H_x^\beta / \partial z$ , and  $\partial H_y^\beta / \partial x$  ( $\beta = x, y, z$ ) components;
- b) a tri-axial transmitter array and three pairs of receiver coils, measuring ~~the~~  $\partial H_z^\beta / \partial z$ ,  $\partial H_x^\beta / \partial z$ , and  $\partial H_y^\beta / \partial z$  ( $\beta = x, y, z$ ) components;

- c) a tri-axial transmitter array and up to 27 pairs of receiver coils, measuring some or all components: of  $\partial H_\alpha^\beta / \partial \gamma (\alpha, \beta, \gamma = x, y, z)$ ;
  - d) three mutually orthogonal transmitter coils, displaced along ~~the~~ a z-axis and oriented in the x-, y-, and z- directions, and three pairs of receiver coils, measuring ~~the~~  $\partial H_z^\beta / \partial x$ ,  $\partial H_x^\beta / \partial z$ , and  $\partial H_y^\beta / \partial x$  ( $\beta = x, y, z$ ) components;
  - e) three mutually orthogonal transmitter coils, displaced along ~~the~~ z-axis and oriented in the x-, y-, and z- directions, and three pairs of receiver coils, measuring ~~the~~  $\partial H_z^\beta / \partial z$ ,  $\partial H_x^\beta / \partial z$ , and  $\partial H_y^\beta / \partial z$  ( $\beta = x, y, z$ ) components;
  - f) three mutually orthogonal transmitter coils, displaced along ~~the~~ z-axis and oriented in the x-, y-, and z- directions, and up to 27 pairs of receiver coils, measuring some or all ~~components:~~ components of  $\partial H_\alpha^\beta / \partial \gamma (\alpha, \beta, \gamma = x, y, z)$ .
3. (Currently Amended) A method for measuring ~~the~~ conductivity of ~~the~~ an anisotropic earth formations penetrated by a wellbore, the method comprising:
- a) measuring a gradient of magnetic field between two closely positioned parallel receiver coils, wherein ~~the~~ a harmonic (frequency domain) electromagnetic field is generated by at least one transmitter coil, and the receiver coils are separated by a small vector,  $\Delta \mathbf{r}$ , with ~~the~~ a magnetic moment direction of the transmitter coil parallel or different from ~~the~~ a magnetic moment direction of the receiver coils, wherein ~~the~~ a distance between two parallel receiver coils being much smaller than ~~the~~ a distance  $L$  between the transmitter and ~~the~~ a center of the vector  $\Delta \mathbf{r}$ , connecting two receivers,

~~$|\Delta r| \ll L$~~ , to ensure that and the receiver pair measures the gradient of the induction magnetic field;

- b) ~~using said gradient electromagnetic induction logging instrument~~ for obtaining a plurality of measurements for different positions ~~of the instrument~~ along the ~~borehole;~~ wellbore;
- c) obtaining from ~~the~~ said plurality of measurements ~~the~~ a horizontal and vertical conductivities of ~~the~~ a medium, and ~~the~~ a relative dip angle of the formation by inverting the gradient electromagnetic induction data using a model of a layered anisotropic formation and regularization methods of inverse problem solution.

4. (Currently Amended) The method of claim 3, ~~wherein the~~ further comprising generating a frequency domain current in the transmitter ~~is generated~~ for at least several frequencies, and the receivers measure ~~the~~ a signal at several frequencies, wherein ~~the~~ multi-frequency gradient measurements are used for frequency gradient EM sounding of the medium at different distances from the wellbore to produce a volume image of ~~the~~ anisotropic conductivity distribution around the borehole.

5. (Currently Amended) A method for measuring ~~the~~ conductivity of ~~the~~ an anisotropic earth formations penetrated by a wellbore, ~~wherein the method comprises:~~ comprising:

- a) measuring a gradient of a magnetic field at ~~the~~ a receiver coil position, wherein ~~the~~ a harmonic (frequency domain) or pulse (time domain) electromagnetic field is generated by two closely positioned parallel transmitter coils, separated by a small vector,  $\Delta r$ , with ~~the~~ a magnetic moment direction of the transmitters parallel or

different from ~~the~~ a magnetic moment direction of the receiver, wherein two transmitters generate successively a harmonic (frequency domain) primary EM field which propagates through the anisotropic formation, surrounding the ~~borehole~~. wellbore;

b) ~~using said gradient electromagnetic induction logging instrument for obtaining a plurality of measurements for different positions of the instrument along the borehole;~~ wellbore;

c) obtaining from ~~the~~ said plurality of measurements ~~the~~ a horizontal and vertical conductivities of ~~the~~ a medium and ~~the~~ a relative dip angle of the formation by inverting ~~the~~ gradient electromagnetic induction data, using a model of layered anisotropic formation and regularization methods of ~~the~~ an inverse problem solution.

6. (Currently Amended) The method of claim 5, ~~wherein the~~ further comprising generating a frequency domain current in the transmitter ~~is generated~~ for at least several frequencies, and the receivers measure ~~the~~ a signal at several frequencies, wherein ~~the~~ multi-frequency gradient measurements are used for frequency gradient EM sounding of the medium at different distances from the wellbore to produce a volume image of ~~the~~ an anisotropic conductivity distribution around the ~~borehole~~. wellbore.

7. (Currently Amended) A method for measuring ~~the~~ conductivity of ~~the~~ an anisotropic earth formations penetrated by a wellbore, ~~wherein the method comprises:~~ comprising:

a) conveying an electromagnetic logging instrument into a ~~borehole~~, wellbore, said logging instrument including a tri-axial EM induction transmitter and a pair of

closely located tri-axial EM induction receivers, separated by a small vector,  $\Delta r$ , wherein one set of tri-axial receivers detects three components of the magnetic field due to each of three transmitters for a total of nine signals forming an induction tensor;

- b) said logging instrument measuring a gradient in the direction  $\Delta r$  of each of three components of the magnetic field in the receivers due to each of three transmitters for a total of nine gradient signals forming a gradient ~~tensor~~; tensor;
- c) using said ~~gradient tensor induction well~~ logging (GTIWL) instrument for obtaining a plurality of measurements for the different positions of the instrument along the ~~borehole~~; wellbore;
- d) obtaining from the said plurality of measurements the horizontal and vertical conductivities of the a medium and the a relative dip angle of the formation by inverting the gradient tensor induction well logging (GTIWL) data using a model of layered anisotropic formation and regularization methods for the an inverse problem solution.

8. (Currently Amended) The method of claim 7, ~~wherein the~~ further comprising generating a frequency domain current in the tri-axial transmitter ~~is generated~~ for at least several frequencies, and the tri-axial receivers measure the a signal at several frequencies, wherein the a multi-frequency measurements are combined in the a gradient tensor induction signal to be used for frequency gradient EM sounding of the medium at different distances from the wellbore to produce a volume image of the anisotropic conductivity distribution around the ~~borehole~~; wellbore.

9. (Currently Amended) A method for measuring the conductivity of ~~the~~ an anisotropic earth formations penetrated by a wellbore, ~~wherein the method comprises:~~ comprising:
- a) conveying an electromagnetic logging instrument into ~~a borehole,~~ the wellbore, said logging instrument including a pair of closely located tri-axial EM induction transmitters, separated by a small vector,  $\Delta \mathbf{r}$ , and a tri-axial EM induction receiver, wherein a set of tri-axial receivers detects three components of ~~the~~ a magnetic field due to each of the three transmitters for a total of nine signals forming an induction tensor;
  - b) measuring by the said logging instrument a gradient in the direction  $\Delta \mathbf{r}$  of each of the three components of the magnetic field in the tri-axial receiver for a total of nine gradient signals forming a gradient ~~tensor:~~ tensor;
  - c) using said ~~gradient tensor induction well logging (GTIWL)~~ instrument for obtaining a plurality of measurements for ~~the~~ different positions of the instrument along the ~~borehole;~~ wellbore;
  - d) obtaining from ~~the~~ said plurality of measurements ~~the~~ horizontal and vertical conductivities of ~~the~~ a medium and ~~the~~ a relative dip angle of the formation by inverting ~~the gradient tensor induction well logging (GTIWL)~~ data using a model of layered anisotropic formation and regularization methods for ~~the~~ an inverse problem solution.
10. (Currently Amended) The method of claim 9, ~~wherein the~~ further comprising generating a frequency domain current in the tri-axial transmitters ~~is generated~~ for at least several frequencies, and the tri-axial receivers measure ~~the~~ a signal at several frequencies, wherein

the multi- frequency measurements are combined in the a gradient tensor induction signal to be used for frequency gradient EM sounding of the medium at different distances from the wellbore to produce a volume image of the anisotropic conductivity distribution around the borehole. wellbore.